

Langfristige HA - Ma 10

Lösungen

1. geg.: $d = 1,90\text{m}$ $\approx r = 0,95\text{m}$ ges.: A_M

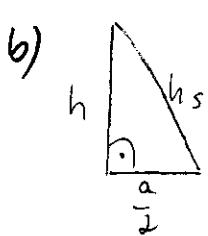
$$h = 3,10\text{m} - 0,6\text{m} = 2,50\text{m}$$

$$A_M = 2\pi rh$$

$$\underline{A_M = 14,92 \text{ m}^2}$$

2. geg.: $a = 3\text{ cm}$ ges.: A_M, A_0, V

$$h_s = 4\text{ cm}$$



$$h_s^2 = h^2 + \left(\frac{a}{2}\right)^2 \quad A_M = 2 \cdot a \cdot h_s$$

$$h^2 = h_s^2 - \left(\frac{a}{2}\right)^2 \quad \underline{A_M = 24 \text{ cm}^2}$$

$$\underline{h = 3,7 \text{ cm}}$$

$$A_0 = A_G + A_M$$

$$V = \frac{1}{3} a^2 \cdot h$$

$$\underline{A_0 = 33 \text{ cm}^2}$$

$$\underline{V = 11,1 \text{ cm}^3}$$

3. geg.: $d = h = 82 \text{ mm} = 8,2 \text{ cm}$

$$g = 7,8 \frac{\text{kg}}{\text{dm}^3}$$

a) $V_Z = \pi r^2 \cdot h \quad V_K = \frac{4}{3} \pi r^3$

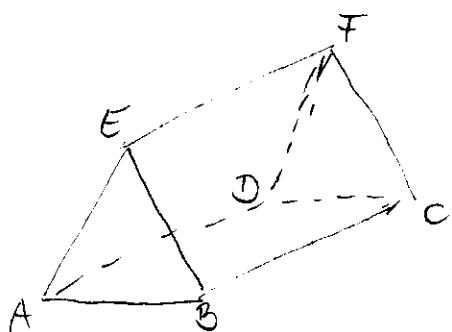
$$V_Z = 433 \text{ cm}^3 \quad V_K = 288,7 \text{ cm}^3$$

$$\rightarrow \text{Abfall } 144,3 \text{ cm}^3 \quad g = \frac{m}{V} \approx m = g \cdot V$$

$$\underline{m = 1125,6 \text{ g}}$$

b) $\frac{144,3 \text{ cm}^3}{433 \text{ cm}^3} = 0,333 \approx \underline{33,3\%}$

4. a)



$$\begin{aligned}
 b) \text{ geg.: } a &= 5 \text{ cm} & V_Q &= a \cdot b \cdot c \\
 b &= 6 \text{ cm} & V_Q &= 90 \text{ cm}^3 \\
 c = h &= 3 \text{ cm} & V_Z &= \pi r^2 h \\
 d = 2 \text{ cm} & \quad r = 1 \text{ cm} & V_Z &= 94 \text{ cm}^3 \\
 g = 7,8 \frac{\text{N}}{\text{dm}^3} & \rightarrow V_K = 80,6 \text{ cm}^3 & m &= g \cdot V = 628,5 \text{ g}
 \end{aligned}$$

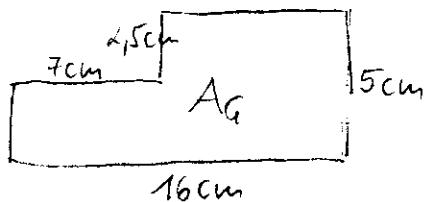
5. geg.: $d_{\text{Ku}} = 120 \text{ mm} = 12 \text{ cm} = d_K = d_Z$ ges.: A₀
 $h_Z = 5 \text{ cm}$ $\rightarrow r = 6 \text{ cm}$ V
 $h_{\text{Ku}} = 16 \text{ cm}$ m
 $g = 8,8 \frac{\text{N}}{\text{dm}^3}$

$$\begin{aligned}
 b) \quad A_{0 \text{ Hku}} &= 2\pi r^2 = 226,2 \text{ cm}^2 \\
 A_{0 \text{ Z}} &= 2\pi r h = 188,5 \text{ cm}^2 \\
 A_{0 \text{ Kue}} &= \pi r s = 322,1 \text{ cm}^2 & s^2 &= r^2 + h^2 \\
 \rightarrow A_0 &= 736,8 \text{ cm}^2 & s &= 17,1 \text{ cm}
 \end{aligned}$$

$$\begin{aligned}
 c) \quad V_{\text{Hku}} &= \frac{2}{3}\pi r^3 = 452,4 \text{ cm}^3 \\
 V_Z &= \pi r^2 h = 94,2 \text{ cm}^3 \\
 V_{\text{Kue}} &= \frac{1}{3}\pi r^2 h = 603,2 \text{ cm}^3 \\
 \rightarrow V &= 1149,8 \text{ cm}^3
 \end{aligned}$$

$$d) \quad m = g \cdot V = 9658,2 \text{ g} \approx \underline{\underline{9,7 \text{ kg}}}$$

6.



$$A_G = (16 \text{ cm} \cdot 5 \text{ cm}) - (2,5 \text{ cm} \cdot 2,5 \text{ cm})$$

$$A_G = 62,5 \text{ cm}^2$$

$$V_P = A_G \cdot h$$

$$\underline{V_P = 1562,5 \text{ cm}^3}$$

$$V_T = 62,5 \text{ cm}^3 \cdot 2 \\ = \underline{125,7 \text{ cm}^3}$$

$$\underline{V_{\text{ges}} = 1436,9 \text{ cm}^3}$$

$$m = g \cdot V = 11380 \text{ g} = \underline{11,38 \text{ kg}}$$

7. geg.: $d_a = 16 \text{ m}$ $\rightarrow r_a = 8 \text{ m}$ ges.: A_o

$$\underline{d_i = 15,96 \text{ m}} \rightarrow r_i = 7,98 \text{ m} \quad V$$

a) $A_o = 4\pi r^2$
 $\underline{A_o = 804,2 \text{ m}^2}$

b) $V = \frac{4}{3}\pi r^3$
 $\underline{V = 2128,6 \text{ m}^3}$

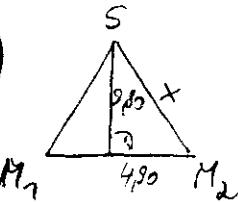
c) $V_a = \frac{4}{3}\pi r^3 = 2144,7 \text{ m}^3$
 $\rightarrow V_{\text{Hölle}} = 16,1 \text{ m}^3 = 16\ 100\ 000 \text{ cm}^3$
 $\rightarrow m = g \cdot V = 127\ 029\ 000 \text{ g}$
 $\underline{m \approx 127 \text{ t}}$

8. geg.: $a = 9,80 \text{ m}$

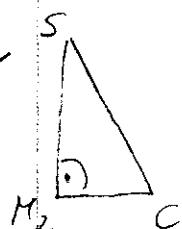
$$h = 9,80 \text{ m}$$

b) $A = 9,80 \text{ m} \cdot 4,90 \text{ m} = \underline{48,02 \text{ m}^2}$

c)


 $x^2 = (9,80 \text{ m})^2 + (4,90 \text{ m})^2$
 $A = \frac{1}{2} \cdot 4,90 \text{ m} \cdot x$
 $\underline{A = 26,85 \text{ m}^2}$

$$x = 10,96 \text{ m}$$



→ sind vier solche Dreiecksflächen

→ $\underline{A = 107,4 \text{ m}^2}$

$$9. \quad a = 11,6 \text{ cm}$$

$$c = 7,6 \text{ cm}$$

$$h_a = 3,6 \text{ cm}$$

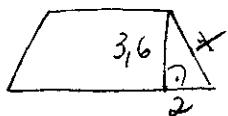
$$h = 10 \text{ cm}$$

$$A_G = \frac{a+c}{2} \cdot h_a$$

$$A_G = 34,56 \text{ cm}^2 \cdot 2 = \underline{\underline{69,12 \text{ cm}^2}}$$

$$A_M = a \cdot h$$

$$\underline{\underline{A_M = 27,4 \text{ cm}^2}}$$



$$x^2 = (3,6 \text{ cm})^2 + (2 \text{ cm})^2$$

$$x = 4,1 \text{ cm}$$

$$\rightarrow u = 27,4 \text{ cm}$$

$$A_O = 2A_G + A_M$$

$$A_O = 34,56 \text{ cm}^2 + 15\% \\ + \underline{\underline{51,47 \text{ cm}^2}}$$

$$\underline{\underline{394,6 \text{ cm}^2}}$$

$$10. \quad \text{geg.: } a = 4 \text{ cm}$$

$$b = \frac{1}{4}a = 1 \text{ cm}$$

$$h = 2a = 8 \text{ cm}$$

$$b) \quad A_Q = a^2 = 16 \text{ cm}^2 \\ A_D = \frac{a \cdot b}{2} = 2 \text{ cm}^2 \quad \left. \begin{array}{l} A_G = A_Q - A_D \cdot 4 \\ = \underline{\underline{8 \text{ cm}^2}} \end{array} \right\}$$

$$V = A_G \cdot h = \underline{\underline{63 \text{ cm}^3}}$$

$$c) \quad V = A_G \cdot h \quad h = 2a \quad A_G = a^2 - 4A_D \quad A_D = \frac{1}{2}a \cdot b$$

$$\hookrightarrow V = A_G \cdot 2a \quad \text{mit } b = \frac{1}{4}a$$

$$\text{folgt } A_D = \frac{1}{8}a^2$$

$$\hookrightarrow A_G = a^2 - 4 \cdot \frac{1}{8}a^2$$

$$A_G = a^2 - \frac{1}{2}a^2$$

$$A_G = \frac{1}{2}a^2$$

$$V = \frac{1}{2}a^2 \cdot 2a$$

$$\underline{\underline{V = a^3}}$$

$$11. \text{ a) geg.: } h_K = 0,33 \text{ m}$$

$$d_K = 1,76 \text{ m} \quad r_K = 0,88 \text{ m}$$

$$A_M = \pi r s$$

$$s^2 = h^2 + r^2$$

$$\underline{A_M = 2,6 \text{ m}^2}$$

$$\underline{s = 0,84 \text{ m}}$$

$$A \text{ für 6 Säulen: } \underline{15,6 \text{ m}^2}$$

$$15,6 \text{ m}^2 \cdot 9\% = 1,4 \text{ m}^2$$

$$15,6 \text{ m}^2 + 1,4 \text{ m}^2 = \underline{17 \text{ m}^2}$$

Der Gesamtbedarf für 6 Dächer beträgt 17 m^2 .

b) geg.: $d_Z = 1,60 \text{ m}$ $r_Z = 0,80 \text{ m}$

$$h_Z = 2,20 \text{ m}$$

$$A_M = 2\pi r h$$

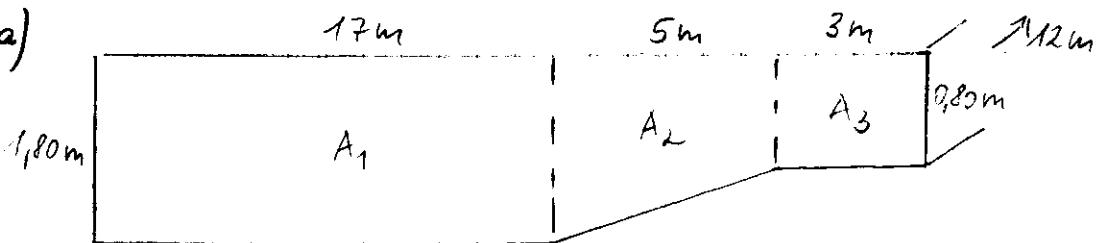
$$A_M = 11,06 \text{ m}^2$$

$$6 \cdot A_M = \underline{66,4 \text{ m}^2}$$

$$66,4 \text{ m}^2 \cdot 9,50 \text{ €/m}^2 = 630,80 \text{ € je Woche}$$

$$\rightarrow \underline{32801,60 \text{ € im Jahr}}$$

12. a)



$$A_1 = 17 \text{ m} \cdot 1,80 \text{ m} \quad A_2 = \frac{1,80 + 0,80 \text{ m}}{2} \cdot 5 \text{ m} \quad A_3 = 3 \text{ m} \cdot 0,80 \text{ m}$$

$$A_1 = 30,6 \text{ m}^2 \quad A_2 = 6,5 \text{ m}^2 \quad A_3 = 2,4 \text{ m}^2$$

$$\hookrightarrow \underline{A_{ges} = 39,5 \text{ m}^2}$$

$$V = A_g \cdot h$$

$$\underline{\underline{V = 474 \text{ m}^3}}$$

Es sind 474 m^3 Wasser enthalten, wenn das Becken bis zum Rand gefüllt ist.

$$6) \quad \begin{array}{l} \text{Rohr 1 : } x+17 \\ \text{Rohr 2 : } x \end{array} \quad \left. \begin{array}{l} \\ \end{array} \right\} 6 \text{ Stunden}$$

$$(x+x+17) \cdot 6 = 474$$

$$12x + 102 = 474$$

$$12x = 372$$

$$\underline{x = 31}$$

$$\underline{x+17 = 48}$$

Aus dem ersten Rohr fließen 48 m^3 und dem zweiten Rohr 31 m^3 Wasser pro Stunde.

$$c) \quad 2 \cdot A_1 = 61,2 \text{ m}^2$$

$$2 \cdot A_2 = 13 \text{ m}^2$$

$$2 \cdot A_3 = 4,8 \text{ m}^2$$

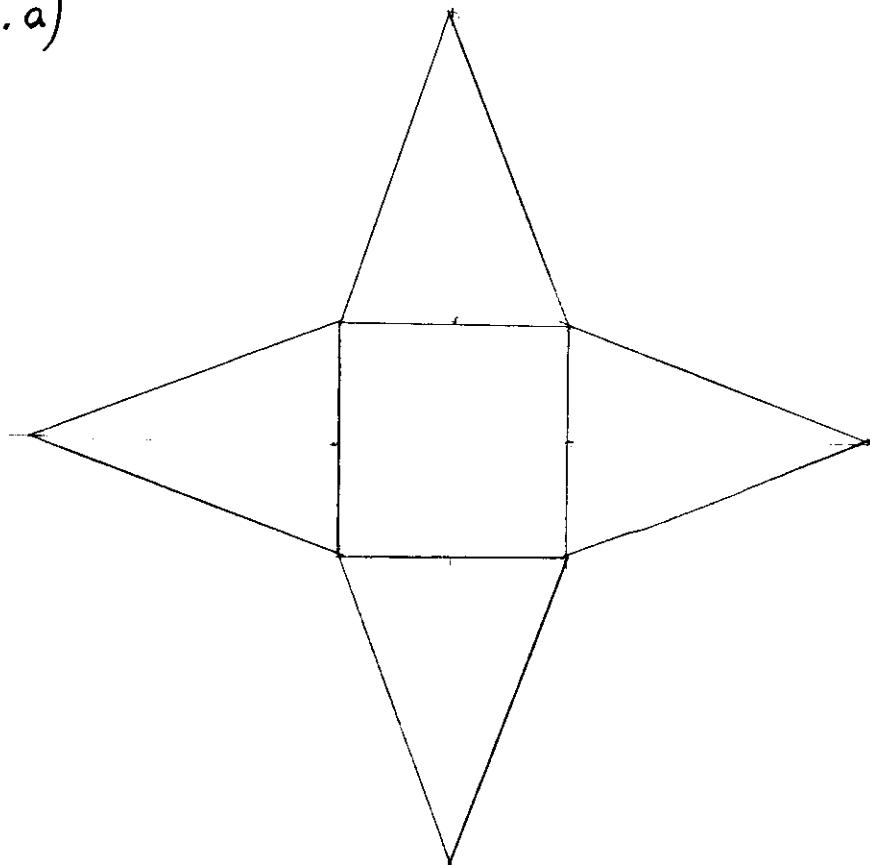
$$A_4 = 1,8 \text{ m} \cdot 12 \text{ m} = 21,6 \text{ m}^2$$

$$A_5 = 0,8 \text{ m} \cdot 12 \text{ m} = 9,6 \text{ m}^2$$

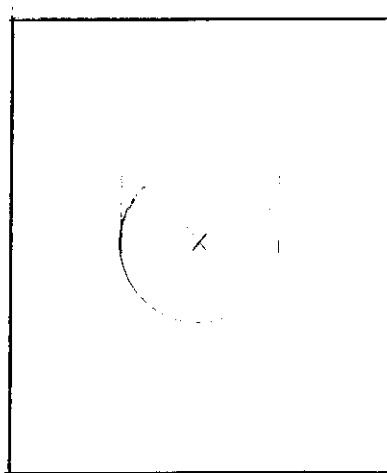
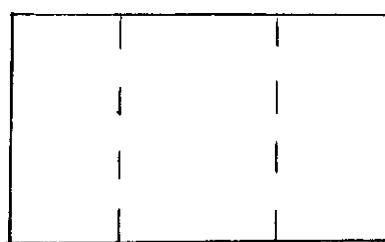
$$\rightarrow \underline{A_{ges} = 110,2 \text{ m}^2}$$

Die zu fließende Fläche beträgt $110,2 \text{ m}^2$

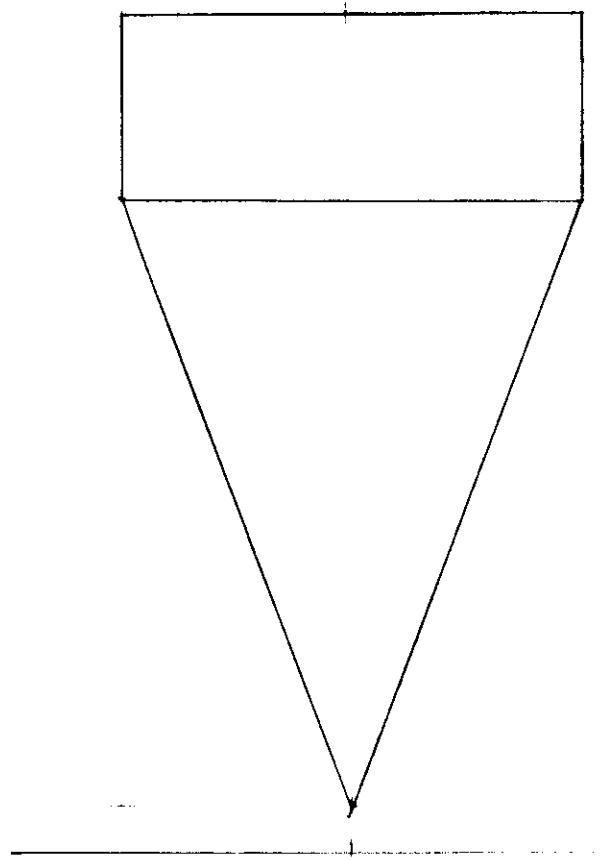
2. a)



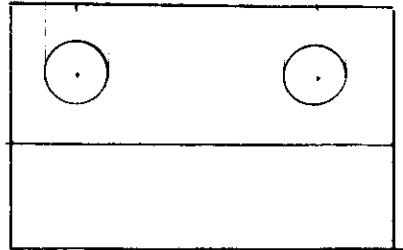
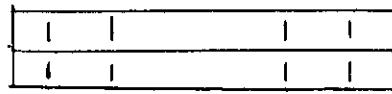
4. b)



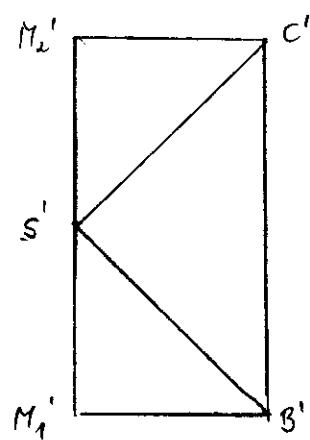
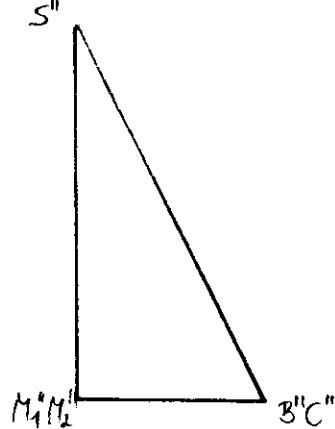
5. Maßstab: 1:2



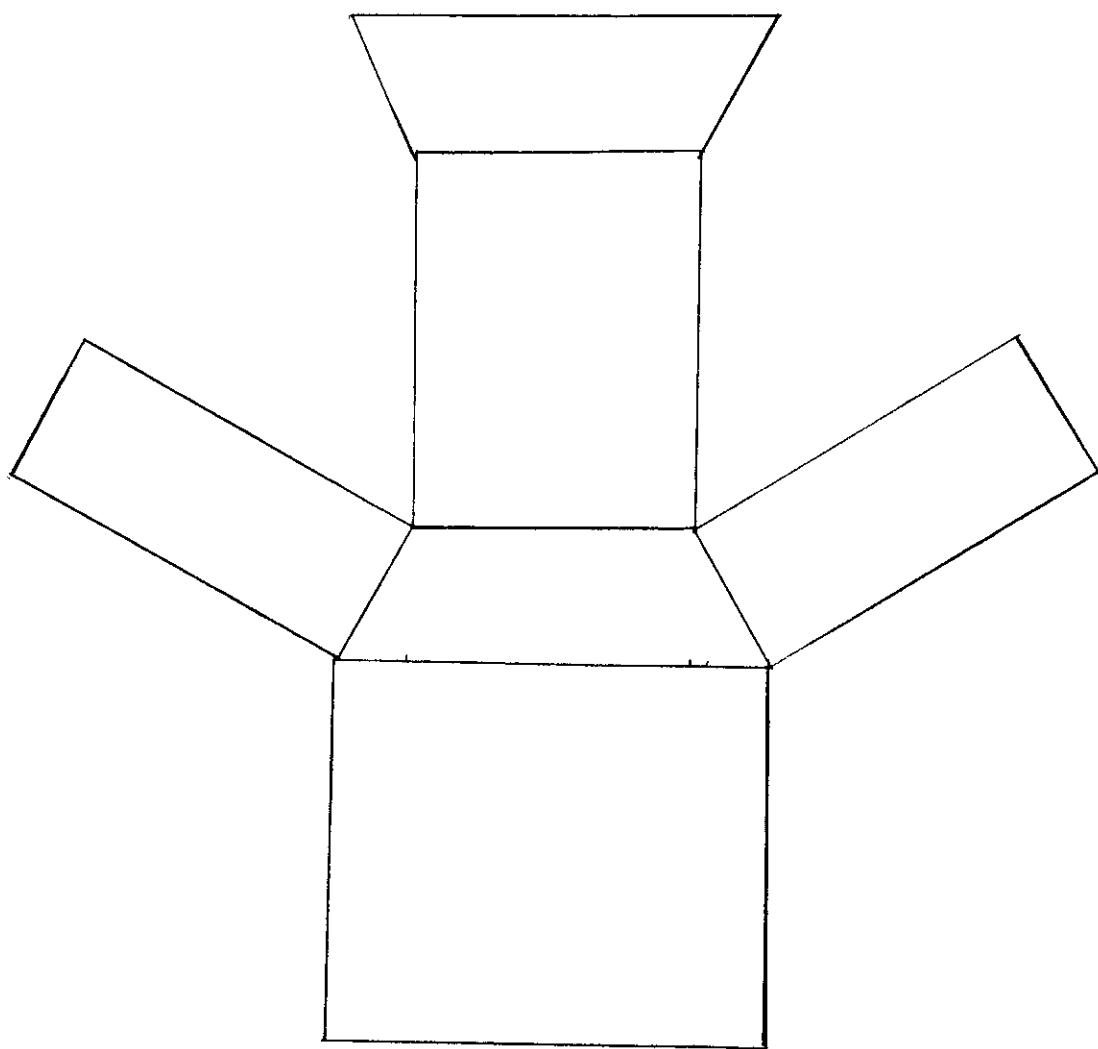
6. a) Maßstab: 1:5



8. a) Maßstab: 1:200



9.a) Maßstab 1:2



10. a)

